

Math 101 — Quiz 1
TUTOR HELP NOT OKAY!!

Name: _____

Directions: **Due Tuesday, Jan. 27th**

- You are not to work on this together or get help from mentors/tutors!!
- Show all work.
- Write your solutions on printer paper.
- Only use a calculator if the question specifically says to use one!
- Box off your solutions.
- No credit will be given for sloppy or illegible work.
- Do not write your solutions on this piece of paper.
- Staple your worked out solutions to this piece of paper and use this piece of paper as your top (or cover) sheet.

Exercises

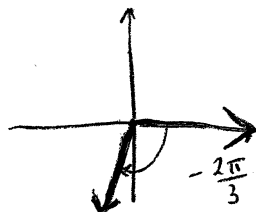
1. Section 2.1

Do problems 20, 28, 30, 42, 54, 92, 94, & 108 on pages 105–106 in the textbook.

2. Section 2.2

Do problems 14, 22, 36, 52, 56, 66, 70, 78, 96 on pages 121–122 in the textbook.

(20)



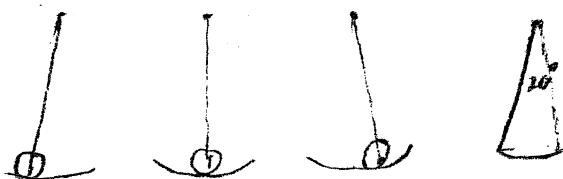
$$\begin{aligned}
 (28) \quad 98^\circ 22' 45'' &= 98^\circ + (22) \cdot (1') + (45) \cdot (1'') \\
 &= 98^\circ + 22 \left(\frac{1}{60}\right)^\circ + 45 \cdot \left(\frac{1}{3600}\right)^\circ \\
 &= \boxed{98.38^\circ}
 \end{aligned}$$

$$\begin{aligned}
 (30) \quad 61.24^\circ &= 61^\circ + 0.24 \cdot (1^\circ) \\
 &= 61^\circ + 0.24 \cdot (60') \\
 &= 61^\circ + 14.4' \\
 &= 61^\circ + 14' + 0.4(1') \\
 &= 61^\circ + 14' + 0.4(60'') \\
 &= \boxed{61^\circ 14' 24''}
 \end{aligned}$$

$$(42) \quad 270^\circ \cdot \frac{\pi}{180^\circ} = \boxed{\frac{3\pi}{2}}$$

$$(54) \quad \frac{5\pi}{12} \cdot \frac{180^\circ}{\pi} = \boxed{75^\circ}$$

(92)

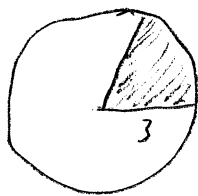


$$\begin{aligned}
 r &= 40 \text{ in} \\
 s &= r\theta = (40 \text{ in}) \left(20^\circ\right) \cdot \frac{\pi}{180^\circ} \\
 &= \frac{40\pi}{9} \text{ in} \approx \boxed{13.96 \text{ in}}
 \end{aligned}$$

(44)

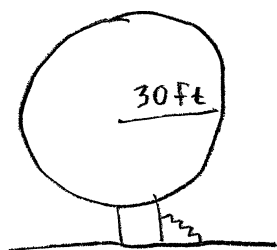
$$r = 3 \text{ cm}$$

$$\theta = 60^\circ$$



$$A = \frac{1}{2} r^2 \theta = \frac{1}{2} (3 \text{ cm})^2 \cdot (60^\circ) \cdot \left(\frac{\pi}{180^\circ} \right) = \frac{3\pi}{2} \text{ cm}^2 \approx \boxed{4.71 \text{ cm}^2}$$

(108)



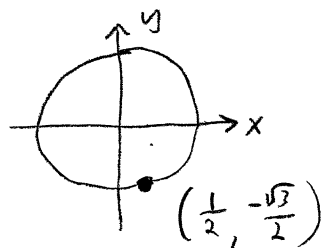
Given $\omega = \text{angular speed} = \frac{1 \text{ rev}}{70 \text{ sec.}}$

Find ω and v .

$$\omega = \frac{1 \text{ rev}}{70 \text{ sec}} \cdot \frac{2\pi}{1 \text{ rev}} = \boxed{\frac{2\pi}{35} \text{ rad/sec}} \quad (\approx 0.8976)$$

$$v = r\omega = (30 \text{ ft}) \left(\frac{2\pi}{35} \text{ rad/sec} \right) = \boxed{\frac{6\pi}{7} \text{ ft/sec}} \approx 2.69 \text{ ft/sec}$$

(14)



$$\cos \theta = \frac{1}{2}$$

$$\sec \theta = 2$$

$$\sin \theta = -\frac{\sqrt{3}}{2}$$

$$\csc \theta = -\frac{2\sqrt{3}}{3}$$

$$\tan \theta = -\sqrt{3}$$

$$\cot \theta = -\frac{\sqrt{3}}{3}$$

$$\tan \theta = \frac{y}{x} = \frac{-\frac{\sqrt{3}}{2}}{\frac{1}{2}} = -\frac{\sqrt{3}}{2} \cdot \frac{2}{1} = -\frac{\sqrt{3}}{1} = -\sqrt{3}$$

$$\sec(\theta) = \frac{1}{x} = \frac{1}{\frac{1}{2}} = 1 \cdot \frac{2}{1} = 2$$

$$\csc(\theta) = \frac{1}{y} = \frac{1}{-\frac{\sqrt{3}}{2}} = 1 \cdot \frac{-2}{\sqrt{3}} = -\frac{2}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$$

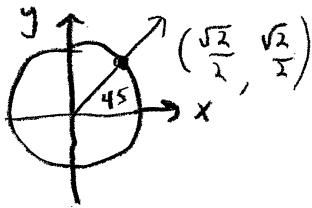
$$\cot \theta = \frac{x}{y} = \frac{\frac{1}{2}}{-\frac{\sqrt{3}}{2}} = \frac{1}{2} \cdot \frac{-2}{\sqrt{3}} = -\frac{1}{\sqrt{3}} = -\frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = -\frac{\sqrt{3}}{3}$$

$$(22) \cos(7\pi) = \boxed{-1}$$

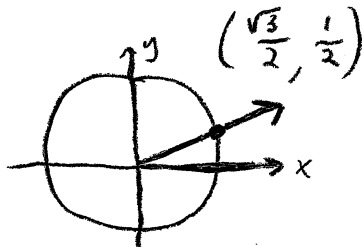


$$\begin{aligned} 7\pi &= 2\pi + 2\pi + 2\pi + 1\pi \\ &= 1\text{ rev} + 1\text{ rev} + 1\text{ rev} + \frac{1}{2}\text{ rev} \\ &= 3\frac{1}{2}\text{ revolutions} \end{aligned}$$

$$(36) \tan 45^\circ \cos 30^\circ = (\tan 45^\circ) \cdot (\cos 30^\circ)$$



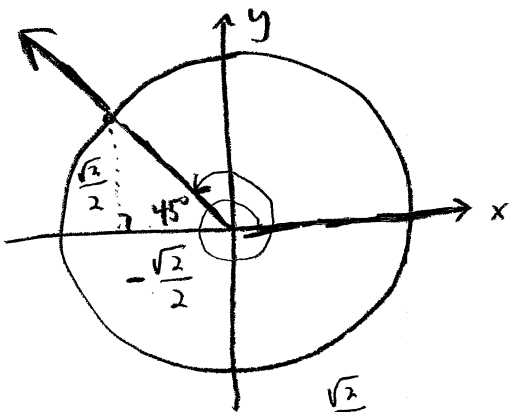
$$= \left(\frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} \right) \cdot \left(\frac{\sqrt{3}}{2} \right)$$



$$= (1) \cdot \left(\frac{\sqrt{3}}{2} \right)$$

$$= \boxed{\frac{\sqrt{3}}{2}}$$

$$(52) \theta = \frac{11\pi}{4}, \quad P(x, y) = \left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} \right)$$



$$\cos \theta = -\frac{\sqrt{2}}{2}$$

$$\sec \theta = -\sqrt{2}$$

$$\sin \theta = \frac{\sqrt{2}}{2}$$

$$\csc \theta = \sqrt{2}$$

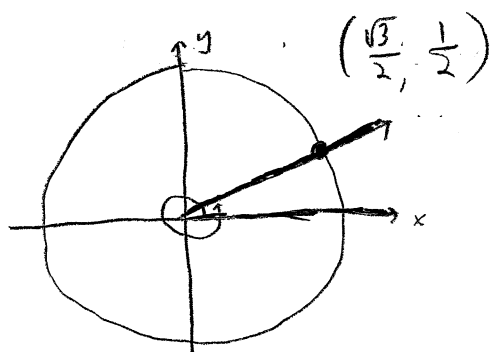
$$\tan \theta = -1$$

$$\cot \theta = -1$$

$$\tan \theta = \frac{y}{x} = \frac{\frac{\sqrt{2}}{2}}{-\frac{\sqrt{2}}{2}} = -1, \quad \cot \theta = \frac{x}{y} = \frac{-\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = -1$$

$$\sec \theta = \frac{1}{x} = \frac{1}{-\frac{\sqrt{2}}{2}} = 1 \cdot \frac{-2}{\sqrt{2}} = -\frac{2}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = -\frac{2\sqrt{2}}{2} = -\sqrt{2}$$

(56) $\theta = 390^\circ$



$$\cos \theta = \frac{\sqrt{3}}{2}$$

$$\sec \theta = \frac{2\sqrt{3}}{3}$$

$$\sin \theta = \frac{1}{2}$$

$$\csc \theta = 2$$

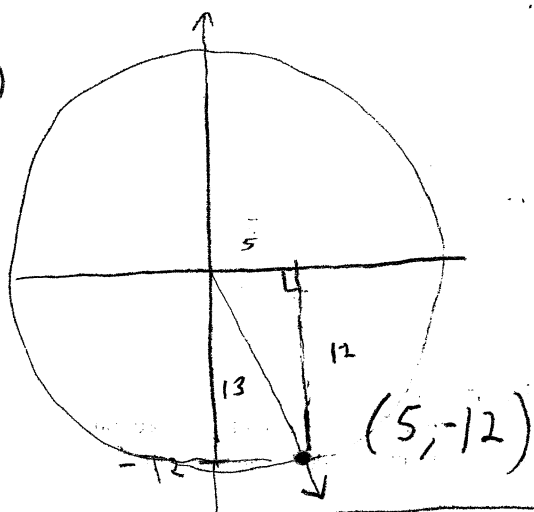
$$\tan \theta = \frac{\sqrt{3}}{3}$$

$$\cot \theta = \sqrt{3}$$

(66) $\cos(14^\circ) \doteq \boxed{0.97}$

(70) $\sin\left(\frac{\pi}{8}\right) \doteq \boxed{0.38}$

(78)



The terminal point is on a circle of radius 13, since

$$r^2 = 5^2 + (-12)^2$$

$$= 25 + 144$$

$$= 169, \text{ or } r^2 = 169, \text{ or}$$

$$r = 13.$$

Then,

$$\cos \theta = \frac{x}{r} = \frac{5}{13}$$

$$\sec \theta = \frac{r}{x} = \frac{13}{5}$$

$$\sin \theta = \frac{y}{r} = \frac{-12}{13}$$

$$\csc \theta = \frac{r}{y} = \frac{13}{-12}$$

$$\tan \theta = \frac{y}{x} = \frac{-12}{5}$$

$$\cot \theta = \frac{x}{y} = -\frac{5}{12}$$

96

$$g(\theta) = g(60^\circ) = \cos(60^\circ)$$

$$= \boxed{\frac{1}{2}}$$

